

## COLUMN DESIGN FOR FLEXURAL (NON DUCTILE-BRACED)

### DESIGN CODE ACI 318-2014

#### General Data

<i>ColumnNo</i>	: C1	
<i>Level</i>	: 16 ft To 32 ft	
<i>FrameType</i>	:= 1	----- 1- for Non Ductile, 2 for Special
<i>B</i>	:= 15 <i>in</i>	----- Width of the Column
<i>D</i>	:= 24 <i>in</i>	----- Depth of the Column
<i>f'c</i>	:= 3.5 <i>ksi</i>	----- Grade of Concrete (Cylindrical Strength)
<i>fy</i>	:= 60 <i>ksi</i>	----- Grade of Main Reinforcement
<i>fyt</i>	:= 60 <i>ksi</i>	----- Grade of Secondary Reinforcement
<i>Cc</i>	:= 2 <i>in</i>	----- Nominal Cover to Beam Tension Reinforcement
<i>Es</i>	:= 29007 <i>ksi</i>	----- Modulus of elasticity of reinforcement
$\phi_{BM}$	:= 0.65	----- Capacity reduction factor for Bending Moment
$\phi_{shear}$	:= 0.75	----- Capacity reduction factor for Shear and torsion
<i>ptmax</i>	:= 4	----- Maximum % reinforcement
<i>ptmin</i>	:= 1	----- Minimum % reinforcement
$\epsilon_{cu}$	:= 0.003	----- Permissible Strain in Concrete
<i>lux</i>	:= 162 <i>in</i>	----- Clear Floor Height along Major Direction@lux
<i>luy</i>	:= 162 <i>in</i>	----- Clear Floor Height along Minor Direction@luy
<i>NoOfFloors</i>	:= 1	----- Number of Floors considered after merged of levels
<i>NoOfColumnsInGroup</i>	:= 1	----- Number of column in Group
<i>ColumnType</i>	:= 1	----- 1- for Braced, 2 for Un-Braced
<i>MinimumEccentricityCheck</i>		----- Simultaneously (Both Axis)
<i>CodeDefinedDBRatio</i>	:= 4	

$$DBRatio := \begin{cases} \text{if } \frac{D}{B} < 4 \\ \quad \text{"DesignAsColumn"} \\ \text{else} \\ \quad \text{"DesignAsWall"} \end{cases} = \text{"DesignAsColumn"}$$

#### Reinforcement Provided

$\phi 1$  := 19.1 *mm*  
 $N1$  := 10  
 $\phi 2$  := 15.9 *mm*  
 $N2$  := 2

$$Ast := \frac{\pi \cdot \phi 1^2}{4} \cdot N1 + \frac{\pi \cdot \phi 2^2}{4} \cdot N2 = 5.057 \text{ in}^2 \quad \text{----- Area of Reinforcement Provided}$$

#### Flexural Design (Analysis Forces)

<i>AnalysisReferenceNo</i>	501
<i>LoadCombination</i>	[9] : 1.5 (LOAD 1: LOAD CASE 1) -1.5 (LOAD 4: LOAD CASE 4 EQ-Y)
<i>CriticalLoacation</i>	Top Joint
<i>Put</i>	:= 109.91 <i>kip</i> ----- Ultimate moment from analysis at Top Node
<i>Muxt</i>	:= 56.62 <i>kip · ft</i> ----- Ultimate moment from analysis along D at Top Node

$M_{uyt} := 157.25 \text{ kip} \cdot \text{ft}$	-----	Ultimate moment from analysis along B at Top Node
$V_{uxt} := -18.29 \text{ kip}$	-----	Ultimate Shear from analysis along D at Top Node
$V_{uyt} := 6.55 \text{ kip}$	-----	Ultimate Shear from analysis along B at Top Node
$M_{ub} := 117.11 \text{ kip}$	-----	Ultimate moment from analysis at Bottom Node
$M_{uxb} := -48.1 \text{ kip} \cdot \text{ft}$	-----	Ultimate moment from analysis along D at Bottom Node
$M_{uyb} := -135.35 \text{ kip} \cdot \text{ft}$	-----	Ultimate moment from analysis along B at Bottom Node
$V_{uxb} := 18.29 \text{ kip}$	-----	Ultimate Shear from analysis along D at Bottom Node
$V_{uyb} := 6.55 \text{ kip}$	-----	Ultimate Shear from analysis along B at Bottom Node

### Sway Calculation (Stability Index)

For\_Global\_X\_Direction

*LoadCombination* [10] : 1.2(LOAD 1: LOAD CASE 1) +0.5 (LOAD 2: LOAD CASE 2)-1.0 (LOAD 3: LOAD CASE 3 EQ-X)

$StoreyHeight(A) := 192 \text{ in}$	-----	Height of Story Considered for design
$GravityLoad(B) := 1499.22 \text{ kip}$	-----	Summation of Axial Load of Story selected
$RelativeDisplacement(C) := 0.47 \text{ in}$	-----	Relative Displacement for Story selected
$StoreyShear(D) := 120.05 \text{ kip}$	-----	Story Shear for Story selected

$$StabilityIndex_Q := \frac{GravityLoad(B)}{StoreyHeight(A)} \cdot \frac{RelativeDisplacement(C)}{StoreyShear(D)} = 0.031$$

$Check :=$	$\begin{cases} \text{if } StabilityIndex_Q \leq 0.05 \\ \quad \text{“Non Sway Frame(Braced)”} \\ \text{else} \\ \quad \text{“Sway Frame(UnBraced)”} \end{cases}$	$= \text{“Non Sway Frame(Braced)”}$	-----	Clause 6.6.4.4.1
			-----	Clause 6.6.4.3

For\_Global\_Y\_Direction

*LoadCombination* [13] : 1.2(LOAD 1: LOAD CASE 1) +0.5 (LOAD 2: LOAD CASE 2)+1.0 (LOAD 3: LOAD CASE 3 EQ-Y)

$StoreyHeight(A) := 192 \text{ in}$	-----	Height of Story Considered for design
$GravityLoad(B) := 1499.22 \text{ kip}$	-----	Summation of Axial Load of Story selected
$RelativeDisplacement(C) := 0.27 \text{ in}$	-----	Relative Displacement for Story selected
$StoreyShear(D) := 120.05 \text{ kip}$	-----	Story Shear for Story selected

$$StabilityIndex_Q := \frac{GravityLoad(B)}{StoreyHeight(A)} \cdot \frac{RelativeDisplacement(C)}{StoreyShear(D)} = 0.018$$

$Check :=$	$\begin{cases} \text{if } StabilityIndex_Q \leq 0.05 \\ \quad \text{“Non Sway Frame(Braced)”} \\ \text{else} \\ \quad \text{“Sway Frame(UnBraced)”} \end{cases}$	$= \text{“Non Sway Frame(Braced)”}$	-----	Clause 6.6.4.3
			-----	

### Effective Length Factor

*EffectiveLengthFactorAlongD* := 1.2

*EffectiveLengthFactorAlongB* := 1.2

### Calculation of Slenderness Check

Along D:

$$EffectiveLengthD := EffectiveLengthFactorAlongD \cdot l_{uy} = 194.4 \text{ in}$$

$$A := D \cdot B = 360 \text{ in}^2 \quad \text{-----} \quad \text{Area of Cross Section}$$

$$I_{xxD} := B \cdot \frac{D^3}{12} = 17280 \text{ in}^4 \quad \text{-----} \quad \text{Moment of Inertia}$$

$$r_D := \sqrt{\left(\frac{I_{xxD}}{A}\right)} = 6.928 \text{ in} \quad \text{-----} \quad \text{Radius of Gyration}$$

$$k_D := EffectiveLengthFactorAlongD = 1.2$$

$$Actual\_Slender\_D := \frac{EffectiveLengthD}{r_D} = 28.059$$

$$M1 := \left\| \begin{array}{l} \text{if } abs(M_{uxt}) > abs(M_{uxb}) \\ \quad \left\| \begin{array}{l} M_{uxb} \\ \text{else} \\ M_{uxt} \end{array} \right\| \end{array} \right\| = -48.1 \text{ kip} \cdot \text{ft}$$

----- Smaller Design Bending Moment at the ends of the the column. Clause 6.2.5.1(b)

$$M2 := \left\| \begin{array}{l} \text{if } abs(M_{uxb}) > abs(M_{uxt}) \\ \quad \left\| \begin{array}{l} M_{uxb} \\ \text{else} \\ M_{uxt} \end{array} \right\| \end{array} \right\| = 56.62 \text{ kip} \cdot \text{ft}$$

----- Higher Design Bending Moment at the ends of the the column. Clause 6.2.5.1(b)

$$LerPerD := \min\left(40, 34 - 12 \cdot \frac{M1}{M2}\right) = 40 \quad \text{-----} \quad \text{Clause 6.2.5.1(b)}$$

$$Check1 := \left\| \begin{array}{l} \text{if } LerPerD > Actual\_Slender\_D \\ \quad \left\| \begin{array}{l} \text{"Column Not Slender Along B"} \\ \text{else if } Actual\_Slender\_D < 100 \\ \quad \left\| \begin{array}{l} \text{"Slender\_Use Approximate method"} \\ \text{else} \\ \text{"Slender\_P-delta effect (revise)"} \end{array} \right\| \end{array} \right\| \end{array} \right\| = \text{"Column Not Slender Along B"}$$

Along B:

$$EffectiveLengthB := EffectiveLengthFactorAlongB \cdot l_{ux} = 194.4 \text{ in}$$

$$A := D \cdot B = 360 \text{ in}^2 \quad \text{-----} \quad \text{Area of Cross Section}$$

$$I_{xxB} := D \cdot \frac{B^3}{12} = 6750 \text{ in}^4 \quad \text{-----} \quad \text{Moment of Inertia}$$

$$r_B := \sqrt{\left(\frac{I_{xxB}}{A}\right)} = 4.33 \text{ in} \quad \text{-----} \quad \text{Radius of Gyration}$$

$$M1 := \begin{cases} \text{if } \text{abs}(M_{uyt}) > \text{abs}(M_{uyb}) \\ \quad || M_{uyb} \\ \text{else} \\ \quad || M_{uyt} \end{cases} = -135.35 \text{ kip} \cdot \text{ft}$$

----- Smaller Design Bending Moment at the ends of the the column. Clause 6.2.5

$$M2 := \begin{cases} \text{if } \text{abs}(M_{uyb}) > \text{abs}(M_{uyt}) \\ \quad || M_{uyb} \\ \text{else} \\ \quad || M_{uyt} \end{cases} = 157.25 \text{ kip} \cdot \text{ft}$$

----- Higher Design Bending Moment at the ends of the the column. Clause 6.2.5

$$\text{Actual\_Slender\_B} := \frac{\text{EffectiveLengthB}}{rB} = 44.895$$

$$\text{LerPerB} := \min\left(40, 34 - 12 \cdot \frac{M1}{M2}\right) = 40$$

----- Clause 6.2.5.1(b)

$$\text{Check1} := \begin{cases} \text{if } \text{LerPerB} > \text{Actual\_Slender\_B} \\ \quad || \text{“Column Not Slender Along B”} \\ \text{else if } \text{Actual\_Slender\_B} < 100 \\ \quad || \text{“Slender\_Use Approximate method”} \\ \text{else} \\ \quad || \text{“Slender\_P-delta effect (revise)”} \end{cases} = \text{“Slender\_Use Approximate method”}$$

### Calculation of Slenderness Moment - Braced (Non-Sway) Frame

Along B:

$$\beta_{dns} := 0.6$$

----- Clause 6.6.4.4.4

$$E_c := \frac{57000}{1000} \cdot \sqrt{\left(\frac{f'c \cdot 1000}{\text{ksi}}\right)} = 3372.165$$

----- Clause 19.2.2.1

$$I_g := D \cdot \frac{B^3}{12} = (6.75 \cdot 10^3) \text{ in}^4$$

----- Moment of Inertia of Section

$$EI := 0.288675 \cdot E_c \cdot I_g = (6.571 \cdot 10^6) \text{ in}^4$$

$$M1_{min} := P_{ub} \cdot (0.6 \cdot \text{in} + 0.03 \cdot B) = 10.247 \text{ kip} \cdot \text{ft}$$

----- Clause 6.6.4.5.4

$$M2_{min} := P_{ub} \cdot (0.6 \cdot \text{in} + 0.03 \cdot B) = 10.247 \text{ kip} \cdot \text{ft}$$

----- Clause 6.6.4.5.4

$$C_m := \begin{cases} \text{if } M2_{min} > M2 \\ \quad || 1 \\ \text{else} \\ \quad || \min\left(\left(0.6 + 0.4 \cdot \left(\frac{M1}{M2}\right)\right), 0.4\right) \end{cases} = 0.256$$

----- Clause 6.6.4.5.3

$$P_c := \pi \cdot \pi \cdot \frac{EI \cdot \text{kip}}{(\text{EffectiveLengthB}^2) \cdot \text{in} \cdot \text{in}} = 1716.046 \text{ kip}$$

----- Clause 6.6.4.4.2

$$\delta := \max\left(1, \frac{C_m}{\left(1 - \frac{P_{ut}}{0.75 \cdot P_c}\right)}\right) = 1$$

----- Clause 6.6.4.5.2

$$Mc1 := \text{sign}(Muyt) \cdot \delta \cdot \max(\text{abs}(Muyt), M1min) = 157.25 \text{ kip} \cdot \text{ft}$$

----- Clause 6.6.4.5.3

$$Mc2 := \text{sign}(Muyb) \cdot \delta \cdot \max(\text{abs}(Muyb), M2min) = -135.35 \text{ kip} \cdot \text{ft}$$

----- Clause 6.6.4.5.3

$$1.4 Muyt = 220.15 \text{ kip} \cdot \text{ft}$$

$$1.4 Muyb = -189.49 \text{ kip} \cdot \text{ft}$$

$$Mc1\_final := \text{sign}(Mc1) \cdot \min(\text{abs}(1.4 Muyt), \text{abs}(Mc1)) = 157.25 \text{ kip} \cdot \text{ft}$$

----- Clause 6.2.5.3

$$Mc2\_final := \text{sign}(Mc2) \cdot \min(\text{abs}(1.4 Muyb), \text{abs}(Mc2)) = -135.35 \text{ kip} \cdot \text{ft}$$

----- Clause 6.2.5.3

### Final Design Forces for Flexural Design

At Top Node:

$$Put = 109.91 \text{ kip}$$

$$Mux := Muxt = 56.62 \text{ kip} \cdot \text{ft}$$

$$Muy := Mc1\_final = 157.25 \text{ kip} \cdot \text{ft}$$

At Bottom Node:

$$Pub = 117.11 \text{ kip}$$

$$Mux := Muxb = -48.1 \text{ kip} \cdot \text{ft}$$

$$Muy := Mc2\_final = -135.35 \text{ kip} \cdot \text{ft}$$

### Final Critical Design Forces

At Top Node:

$$Put = 109.91 \text{ kip}$$

$$Mux\_Final := Muxt = 56.62 \text{ kip} \cdot \text{ft}$$

$$Muy\_Final := Mc1\_final = 157.25 \text{ kip} \cdot \text{ft}$$

### $\phi Pn$ , Max Check

$$fy\_1 := fy = 60 \text{ ksi}$$

----- Clause 22.4.2.1

$$\text{LoadCombination} \quad [2]: 1.2 (\text{LOAD 1: LOAD CASE 1}) + 1.6 (\text{LOAD 2: LOAD CASE 2})$$

$$\text{CriticalLocation} \quad \text{Bottom Joint}$$

$$Pu := 863.41 \text{ kN}$$

----- Factored Axial force

$$Mux1 := -188.66 \text{ kip} \cdot \text{ft}$$

----- Factored Bending Moment along Major Direction

$$Muy1 := -37.88 \text{ kip} \cdot \text{ft}$$

----- Factored Bending Moment along Minor Direction

$$Ag := B \cdot D = 360 \text{ in}^2$$

----- Cross Section Area

$$Ast = 5.057 \text{ in}^2$$

----- Area of Reinforcement Provided

$$pt := \frac{Ast \cdot 100}{Ag} = 1.405$$

----- % Reinforcement Provided

$$\phi Pnmax := 0.8 \cdot \phi BM \cdot (0.85 \cdot f'c \cdot (Ag - Ast) + (Ast \cdot fy\_1)) = 706.864 \text{ kip}$$

----- Clause 22.4.2.2

$$\text{Check} := \left\| \begin{array}{l} \text{if } Pu \leq \phi Pnmax \\ \quad \left\| \begin{array}{l} \text{"Ok"} \\ \text{else} \\ \text{"Revise"} \end{array} \right\| \\ \end{array} \right\| = \text{"Ok"}$$

## Minimum Ast Calculation

$$f_y_2 := f_y = 60 \text{ ksi} \quad \text{-----} \quad \text{Clause 22.4.2.1}$$

*LoadCombination* [2]: 1.2 (LOAD 1: LOAD CASE 1) + 1.6 (LOAD 2: LOAD CASE 2)

$$P_u_{max} := 156.37 \text{ kip}$$

$$A_{stReq} := \frac{0.442 \cdot f'_c \cdot A_g - P_u_{max}}{(0.442 \cdot f'_c) - (0.52 \cdot f_y_2)} = -13.508 \text{ in}^2 \quad \text{-----} \quad \text{Clause 22.4.2.2}$$

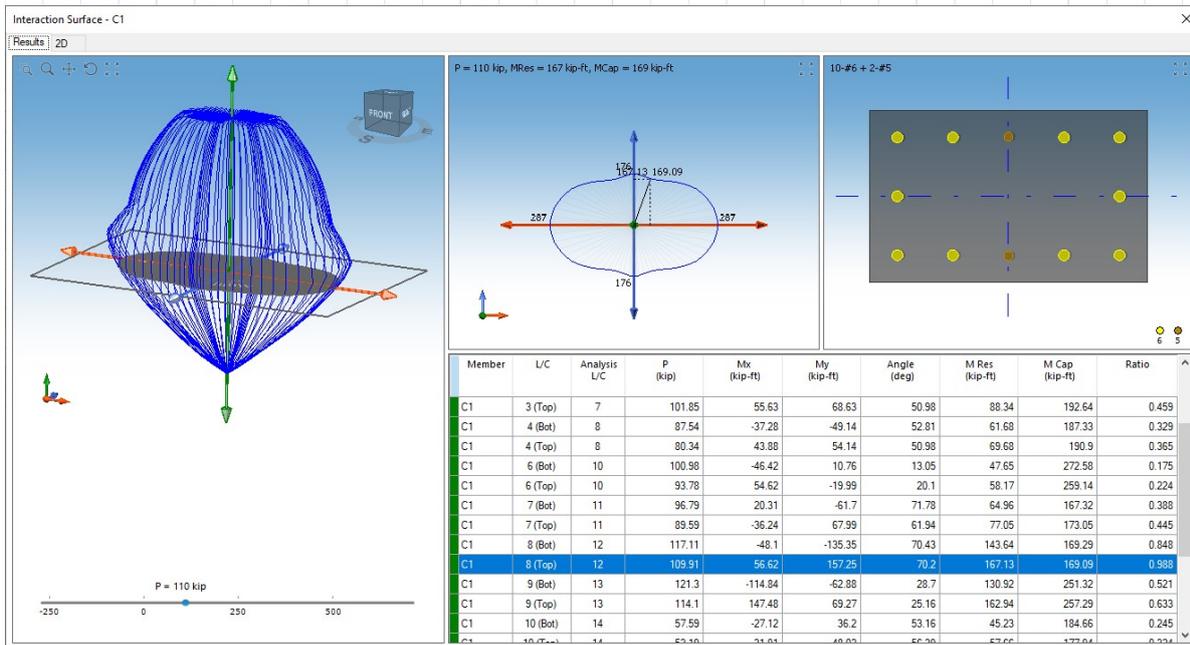
$$pt := \begin{cases} \text{if } A_{stReq} \leq 0 \\ \quad \quad \quad 0 \\ \text{else} \\ \quad \quad \quad \frac{A_{stReq}}{A_g} \end{cases} = 0$$

$$pt_{min} := \max(0.5, pt) = 0.5 \quad \text{-----} \quad \text{Clause 10.3.1.2}$$

$$UserDefinedpt := 1$$

$$Finalpt := \max(pt_{min}, UserDefinedpt) = 1$$

## PM Curve



## Resultant Moment (Combined Action)

### Moment Capacity Check

$$P_{tcalculated} := \frac{A_{st} \cdot 100}{A_g} = 1.4 \quad \text{-----} \quad \text{\% Reinforcement Provided}$$

$$LoadAngle := 39.8 \quad \text{-----} \quad \tan^{-1} (M_{uy\_Final} / M_{ux\_Final})$$

$$M_{res} := \sqrt{M_{ux\_Final}^2 + M_{uy\_Final}^2} = 167.133 \text{ kip} \cdot \text{ft} \quad \text{-----} \quad \text{Resultant Bending Moment}$$

$\phi Mcap := 169.08 \text{ kip} \cdot \text{ft}$  ----- Moment Capacity from PM Curve

$CapacityRatio := \frac{Mres}{\phi Mcap} = 0.988$  ----- Clause 10.4.2

Check :=  $\left\{ \begin{array}{l} \text{if } CapacityRatio < 1 \\ \quad \text{“Ok”} \\ \text{else} \\ \quad \text{“Revise”} \end{array} \right\} = \text{“Ok”}$  ----- Clause 10.4.2

Design Data for All Load Combination

C1  
 Level : 16 ft To 32 ft  
 Frame Type = Non-Ductile  
 Design Code = ACI 318 - 14  
 Grade Of Concrete (f'c) = 3.5 ksi  
 Grade Of Steel (Main) = 60 ksi  
 Grade Of Steel (Shear) = 60 ksi  
 Column B = 15 in  
 Column D = 24 in  
 Clear Cover = 2 in  
 Pt = 1.4 %

Design Table :

Member	LOC	L/C	Analysis L/C No	Pu	Analysis			Mslr or MC		Design			Mcap	Capacity Ratio
					Mx	My		Mx	My	Mux	Muy	MuRes		
				(kip)	(kip-ft)	(kip-ft)	(kip-ft)	(kip-ft)	(kip-ft)	(kip-ft)	(kip-ft)	(kip-ft)		
41	BOT	1	5	102.13	-43.49	-57.33	-	-57.33	-43.49	-57.33	71.96	188.48	0.382	
41	TOP	1	5	93.72	51.19	63.16	-	63.16	51.19	63.16	81.3	191.93	0.424	
41	BOT	2	6	156.37	-69.22	-91.24	-	-91.24	-69.22	-91.24	114.52	191.41	0.598	
41	TOP	2	6	149.16	81.47	100.52	-	100.52	81.47	100.52	129.39	195.2	0.663	
41	BOT	3	7	109.05	-47.26	-62.29	-	-62.29	-47.26	-62.29	78.19	189.02	0.414	
41	TOP	3	7	101.84	55.62	68.63	-	68.63	55.62	68.63	88.34	192.64	0.459	
41	BOT	4	8	87.54	-37.28	-49.14	-	-49.14	-37.28	-49.14	61.68	187.33	0.329	
41	TOP	4	8	80.34	43.88	54.14	-	54.14	43.88	54.14	69.68	190.9	0.365	
41	BOT	6	10	100.98	-46.42	10.76	-	10.76	-46.42	10.76	47.65	272.58	0.175	
41	TOP	6	10	93.78	54.63	-19.99	-	-19.99	54.63	-19.99	58.17	259.14	0.224	
41	BOT	7	11	96.79	20.31	-61.71	-	-61.71	20.31	-61.71	64.96	167.32	0.388	
41	TOP	7	11	89.59	-36.24	67.99	-	67.99	-36.24	67.99	77.04	173.05	0.445	
41	BOT	8	12	117.11	-48.1	-135.35	-	-135.35	-48.1	-135.35	143.64	169.29	0.848	
41	TOP	8	12	<b>109.91</b>	56.62	157.25	-	157.25	56.62	157.25	167.13	169.08	0.988	
41	BOT	9	13	121.3	-114.84	-62.88	-	-62.88	-114.84	-62.88	130.92	251.32	0.521	
41	TOP	9	13	114.1	147.48	69.27	-	69.27	147.48	69.27	162.94	257.29	0.633	
41	BOT	10	14	57.59	-27.12	36.2	-	36.2	-27.12	36.2	45.23	184.66	0.245	
41	TOP	10	14	52.19	31.91	-48.02	-	-48.02	31.91	-48.02	57.65	177.94	0.324	
41	BOT	11	15	53.4	39.61	-36.27	-	-36.27	39.61	-36.27	53.71	202.84	0.265	
41	TOP	11	15	48	-58.95	39.96	-	39.96	-58.95	39.96	71.22	216.64	0.329	
41	BOT	12	16	73.72	-28.8	-109.91	-	-109.91	-28.8	-109.91	113.62	162.42	0.7	
41	TOP	12	16	68.31	33.9	129.22	-	129.22	33.9	129.22	133.59	161.05	0.83	
41	BOT	13	17	77.91	-95.53	-37.44	-	-37.44	-95.53	-37.44	102.61	250.36	0.41	
41	TOP	13	17	72.51	124.77	41.24	-	41.24	124.77	41.24	131.41	252.53	0.52	