



NOTES ON THE APPLICATION OF THE SPRING

AGENTS

Plaxis B.V. appointed a third agent in the U.S.A. From May 1st the company GEMSoft (Geotechnical Engineering Modeling Software) will be an official Plaxis agent for the U.S.A. GEMSoft is located in the Central part of the U.S.A. with offices in Chicago, IL and Houston, TX.

The Houston office is headed up by Kenneth E. Tand, and the Chicago office by Erik G. Funegard. Both Erik and Kenneth have long backgrounds in geotechnical engineering with a strong focus on the petrochemical industry.

Kenneth holds a Master's degree in Civil Engineering from the University of Houston and has been a practicing geotechnical engineer for over 35 years. Ken has been a Plaxis user for over 10 years and has published several papers on the use of Plaxis to solve difficult geotechnical problems.

Erik holds a M.Sc. in Civil Engineering from the Royal Institute of Technology in Stockholm Sweden, as well as an MBA from the University of Chicago. Erik was the chief geotechnical engineer for a major international oil company for over 10 years with first-hand experience of the use of advanced analysis techniques to reduce construction costs.

All three agents can act, as agent for the whole U.S.A. but GemSoft will primarily work in the central U.S.A. The Plaxis agent for mainly the West part of the U.S.A., C. Felice & Company, LLC with its headquarter in Kirkland, Washington has been merged with LACHEL & Associates, Inc. The new firm will be known as LACHEL FELICE & Associates, Inc. For contact details of GemSoft, Lachel Felice and the long-term Plaxis agent in the East of U.S.A., GeoComp see our website.

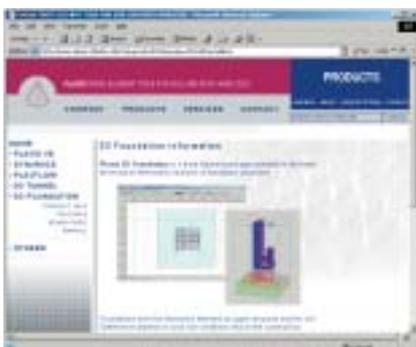
TERRASOL celebrates its 25th anniversary! This event will take place in Paris-La Défense on September 28th 2004. TERRASOL was founded in 1979, and has regularly grown up since (more than 30 people today) as a leading geotechnical consulting company, working in fields like foundations, tunneling, maritime works, excavations, earth-works, infrastructures, etc.

TERRASOL has always used its geotechnical know-how and expertise to develop and sell its own software. It became PLAXIS' agent for France in 1998, and now participates in the PDC program and Plaxis Advisory Board. Its software department also provides services like technical support and continuing education.

REVISED WEBSITE

A revised website is launched to disseminate information more transparently. We hope we have created an informative Website that makes life easier for the Plaxis users and others. News, product and course information is easy to find and updates are easy to access.

Any additional suggestions are welcome; please send them to a.bregman@plaxis.nl.



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INTRODUCTION

The use of a spring constant for the design and analysis of raft and pile-raft foundations has many limitations, related to the proper estimation of the spring constant magnitude and the soil structure interaction. Spring constants have been used for example in the design of a Mass Rapid Transit railway station in an oversea project. The overview of soil condition on that particular site is as shown in Fig. 1 below.

At this project the spring constant concept was adopted for designing the station raft foundation. The structural engineer asked for the magnitude of the spring constant from a young geotechnical engineer, who then gave a coefficient of subgrade reaction (in kN/m³) derived from a plate-loading test. This parameter was later converted into a foundation coefficient of subgrade reaction, k_s, by using the following equation:

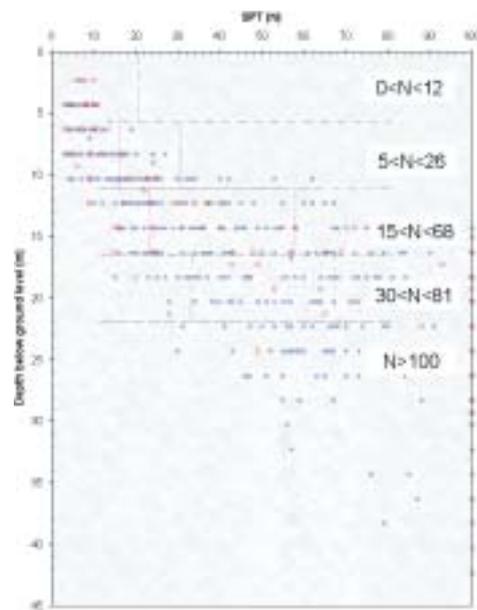


Figure 1: SPT vs Depth

$$k_s = k \left[\frac{B + 0.3}{2B} \right]^2 \tag{1}$$

where B is the width of the raft foundation.

This last parameter was then applied as a spring constant by multiplying it with the unit area under the raft foundation (the unit dimension became kN/m). A certified Professional Engineer then approved the outcome of the raft foundation design for construction. Without prejudice to blame others, it is obviously a mistake! Why it is so? For B greater than 0.3 m, equation 1 clearly shows that the greater the value of B the smaller the value of k_s. While it is structurally correct that the wider the foundation the more flexible the foundation is. It does not equally right for the foundation soil. The engineers had missed the fact that the soil at that area was far from homogeneous.

CONSTANT AND SOIL-STRUCTURE INTERACTION PROBLEMS

The soil condition shows that, within the influence of the raft foundation, the deeper the foundation soils the harder they are. This means the deeper soils have greater rigidity as compared to the layer right below the raft foundation (note: the width of the raft is around 35 m).

The inappropriate spring constant led to an excessive settlement of the raft. As a result, in order to reduce the settlement, the center of the raft was strengthened with more than 20 number of bored piles. Upon reviewing the design, the author proved that the bored piles were excessive and unnecessary. However, by the time it was found, it was too late.

The above case shows the application of spring constant without considering the characteristics and the behavior of the underlying soils. And it is also an example of the existence of ignorance, gaps and weakness in the relation among the structural and geotechnical engineers. This papers tries to elaborate the underlying principle the spring constant theory, its limitation and the application of specially made geotechnical software to solve the problem of soil structure interaction.

SPRING CONSTANT - THE THEORETICAL BACKGROUND AND THE LIMITATION

“What is the spring constant at this particular site?” or “What is the modulus of subgrade reaction at this location?” is a common question asked by a structural engineer to a geotechnical engineer. It is a straightforward question. Unfortunately, it has no direct, let alone a simple answer.

The concept of spring constant was first introduced by Winckler in 1867. He modeled flexible foundation, such as raft, to stand on an independent discreet spring elements or supports. In 1955, Karl Terzaghi, in his paper ‘*Evaluation of coefficients of subgrade reaction*’ proposed a method to estimate the magnitude of the spring constants. His approach, also known as subgrade reaction model, was then became popular and commonly used in the design of raft foundation.

Looking back into the origin of this concept (see Fig.2), one can see that the modulus or the coefficient of subgrade reaction, $k_s(x)$, is defined as the foundation pressure, $p(x)$, divided by the corresponding settlement of the underlying soil, $d(x)$, i.e.:

$$k_s(x) = \frac{p(x)}{d(x)} \tag{2}$$

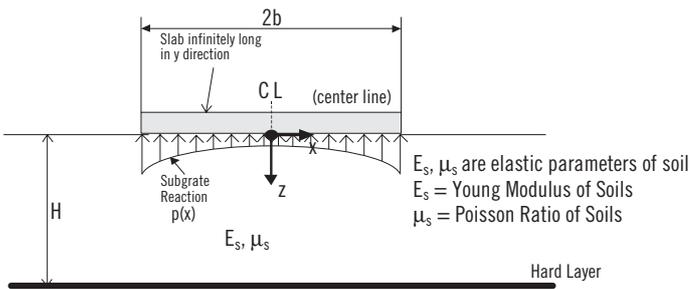


Figure 2: Subgrade Reaction under a Flexible Foundation

In other words, the subgrade reaction is no other than the distribution of soil reaction, $p(x)$, beneath the raft foundation structure against the foundation load. The distribution of the soil reaction is not linear in shape. This is particularly true when the foundation is subjected to uniform load. In this case, generally, the distribution of the soil reaction in clayey soils is curving upward, as shown in Fig. 2, with the largest reaction around the edges of the foundation and the smallest reaction around the center. In sandy soils, the reverse reaction is seen, i.e. zero on the edges and maximum at the center point. In principle, the distribution of the soil reactions right beneath the raft foundation depend on the position of the point under consideration (i.e., the distance of x), the shape of the loading and the relative rigidity (EI) of the raft foundation structure against the underlying soils.

The Winckler model is a simplified mathematical formulation of an elastic soil model. This concept does not take into account the fact that the foundation reaction or the soil stresses is distributed to the deeper soil layer and forming the so called ‘bulb pressure’. The soil settlement beneath the foundation is the accumulation of interactions between the soil stresses and the elastic parameters of the soils at each point inside the bulb pressure zone. Assuming the soils inside the bulb pressure zone posses are homogeneous, Vesic (1961) expanded the Winckler model into elastic model and developed the following equation:

$$k_s = \frac{E_s}{B \cdot I_p \cdot (1 - \nu_s^2)} \tag{3}$$

The above Vesic's equation clearly shows that the modulus of subgrade reaction depends not only on the width of the foundation, B , but also on the elastic parameters of soils, E_s and μ_s , and on the shape factor of the foundation, I_p .

In the earlier days, for the sake of mathematical simplicity, it is generally simplified that the spring constant is not a function of the position x (see Fig.2), hence a single value of spring constant is applied. However, the non-linearity distribution of the soil reactions right beneath the foundation structure suggests that the so-called modulus of subgrade reaction, hence the spring constant, is not a unique value. Terzaghi himself recognized the limitation of this assumption. Bowles (1997) suggested providing higher k_s at the edges of the raft and smaller k_s at the center position.

The above explanations show that there is no discrete value of modulus of subgrade reaction for a given type of soil. Therefore, it does not realistic to ask for a spring constant value without the information on the type and the size of the foundation structure.

In layered soils with different elastic parameters, an equivalent model must be developed in order to derive a representative modulus of subgrade reaction. To do this the elastic settlement of the layered soils induced by the foundation pressure must first be calculated. Poulos and Davis, 1974, mathematical formulation can be used to calculate the elastic settlement of the foundation soils. In a pile raft foundation, to answer the question on the magnitude of the spring constant, the geotechnical engineer also has either to calculate the settlement of the pile foundation or derives it from a pile load test result.

Since the modulus of subgrade reaction (spring constant) is needed to calculate the settlement of the foundation soils, why should one goes to the trouble in providing the spring constant? The structural engineers asked the spring constant because they want to feed in the parameter into their computer software. To the author knowledge, as it is not developed to handle geotechnical problems, the structural engineering software used in analyzing raft or pile raft foundation cannot handle geotechnical parameters.



Another limitation of the spring constant model is the assumption that the foundation soil has linear or elastic behavior. In reality, since Winckler introduced his theory (1867) 133 years have lapsed, and the geotechnical engineering has kept on advancing. It has been known that soil behavior does not elastic. It is an elastoplastic material with different behavior within each classification, and many soil models have been developed.

PROPER SOIL MODEL AND SOIL STRUCTURE INTERACTION

In order to provide a relatively simple and quick solution for the analysis of raft foundation, Winckler followed by Terzaghi, simplified the mathematical formulation into the spring constant or modulus of subgrade reaction model. Over the time, many geotechnical experts had gained better and better understanding on soil behavior and many soil models has been developed. Many of them come with complex mathematical equations, which needs more advanced computer technology and special finite element software to solve.

Until late 1980s where computer hardware, software and run time cost was still very expensive, the spring constant model was indeed one of a good tool for engineers. However, since mid of 1990s and especially as we enter this new millenium, advanced Personal Computer and the relevant geotechnical engineering software has become available and affordable for most firm. So why don't we use a specific finite element method to solve a soil structure interaction problem? Nowadays, finite element software, such as PLAXIS, CRISP, SIGMA, etc., which is specially developed to solve geotechnical problems has been available. T

CASE STUDY ON SOIL STRUCTURE INTERACTION

In a densely populated city, it is not uncommon that a subway tunnel must be constructed underneath an existing building foundation or the reverse, that is to construct a building on top of an existing tunnels. In 1998, the author had a chance to evaluate such a problem. At that time a twin tunnel subway project was on its way. These 6.3 m diameter twin tunnels shall cross some 30 m underneath a land where a condominium building was planned. The landlord was wondering when to construct his building, before or after the tunneling?

If the building was constructed before the tunnels passed the area, he had no responsibility on the tunnel construction and it would be the tunnel contractor responsibility to take precaution not to induce any negative impact to the building. However, at that time the macro economy situation was not favorable for the sales of the condominium. On the other hand, if the building was constructed later, the impact of the building construction to the twin tunnels had to be studied. And this might lead to a more costly foundation, as there is a requirement that any pile foundation from the ground surface to the spring-lines of a subway tunnel must not bear any friction resistance. The other option available is to strengthen the tunnel lining to anticipate the future additional stresses that come from the building foundation. And the building owner would have to contribute on its cost.

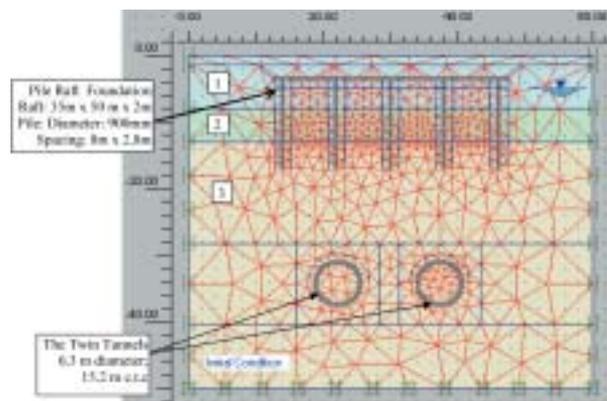


Figure 3: The Finite Element Model of The Initial Condition

Figure 3 shows the initial condition of the site and the subsequent soil parameters. The center of the tunnel lines is 35 m below the ground surface. Landscaping of the site required a 1.5 m excavation and this was done before the tunneling. The base of the raft foundation would be around 3.5 m from the ground surface. The groundwater level was found at about 3.75 m below the ground surface. Table 1 shows the soil data. Mohr-Coulomb soil model was adopted to perform the analysis.

Mohr-Coulomb	Identification	Type	γ_{dry} (kN/m ³)	γ_{sat} (kN/m ³)	i_{vol} (initial)	i_{vol} (initial)	ν	E_{ref} (kN/m ²)
1	soft silty clay	Drained	16.0	18.8	1.300E-3	9.000E-4	0.33	30000.0
2	hard silty clay	Drained	16.0	20.8	1.300E-3	9.000E-4	0.33	60000.0
3	sandstone	Drained	19.0	21.8	0.0100	0.0006	0.33	1E5

Number	Identification	c_{int} (kN/m ²)	ϕ (°)	ϕ (°)	γ_{vol} (-)	Interface Permeability
1	soft silty clay	5.0	22.0	0.0	0.70	Neutral
2	hard silty clay	30.0	38.0	0.0	0.70	Neutral
3	sandstone	75.0	42.0	5.0	0.80	Impermeable

Table 1: The Soil Data

Many possible construction sequences were analyzed. The construction sequence presented in this paper is as follows:

- Overall excavation up to 1.5 m deep.
- Bored piles construction
- Tunneling (followed by volume loss)
- 2.0 m excavation for raft construction
- Raft construction
- Building Construction and Load Application

The results of the final stage construction are presented below.

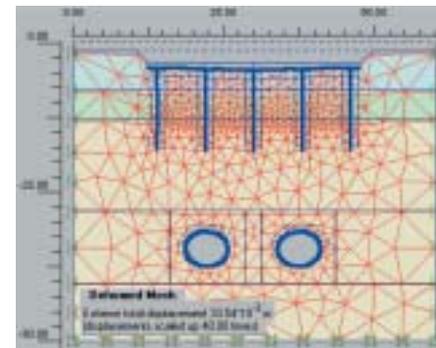


Figure 4: Deformed Mesh

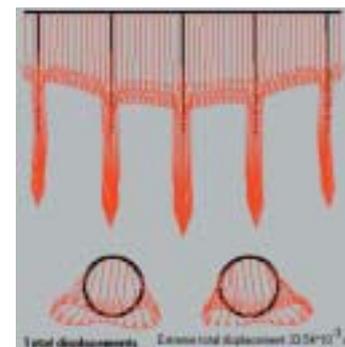


Figure 5: Pile Raft and Tunnels Total Displacement

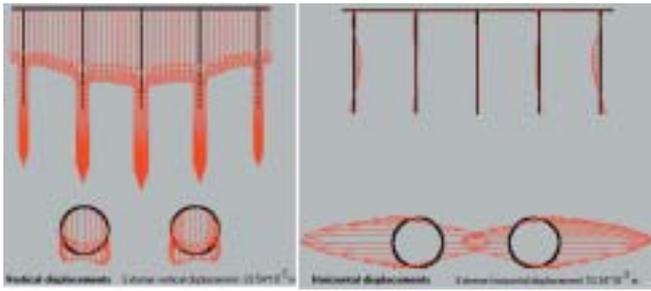


Figure 6: Pile Raft and Tunnels Vertical and Horizontal Displacement

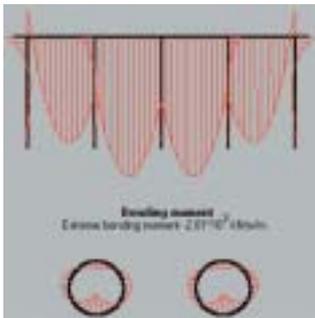


Figure 7: Pile Raft and Tunnels Bending Moment

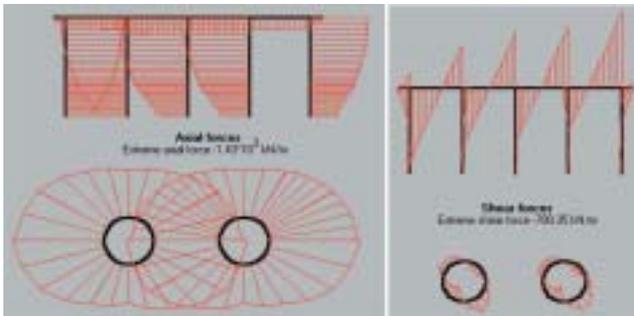


Figure 8: Pile Raft and Tunnels Axial and Shear Forces

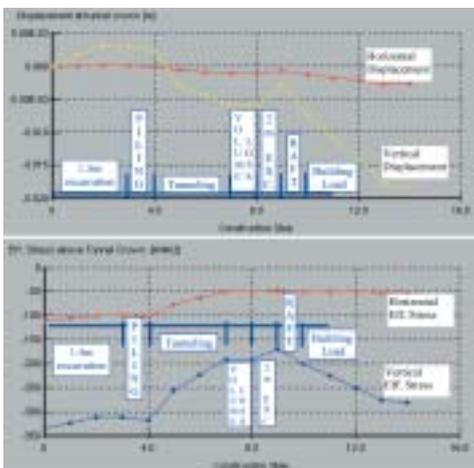


Figure 9: Changes of Stress and Displacement right above Tunnel Crown

With the said construction sequence, the result of the analysis shows that the maximum pile raft settlement would be in the order of 33 mm. The analysis also predicted that the building would exert additional vertical stress of 90 kN/m², with a corresponding 12 mm vertical displacement, to the tunnel crown. The above example was one of the input for project evaluation. It shows the importance of the soil structure interaction analysis, which cannot be solved by using the spring constant model.

CONCLUSIONS

The above discussions show that there is no straightforward answer to the question of: "What is the magnitude of the spring constant (or the modulus of subgrade reaction) at this site?" It is inappropriate for a geotechnical engineer to provide the said parameters without knowing the system and the size of the foundation. The non-linearity of soil reaction beneath a footing or raft foundation suggests that the k_s value is not a unique value. Great care must be exercised in deriving the value. It is always important to have a good communication, understanding and cooperation between the structural engineer and the geotechnical engineer in solving a particular foundation problem.

Since the computer technology and the relevant finite element software has become relatively cheap and readily available, whenever possible, it is suggested to perform a soil structure interaction analysis and leave behind the spring constant concept. As demonstrated above, nowadays, the geotechnical finite element software is capable to handle complex soil structure interaction problem, which cannot be solved by the spring constant model.

Last but not least, the derivation of the input soil parameters is very important. As soil is not manmade materials, strong theoretical knowledge and sophisticated engineering software alone is not adequate.

A geotechnical engineer must gain plenty of practical experiences in order to come out with a sound engineering judgment in determining the relevant soil parameters for a particular soil model. It does not matter how sophisticated computer software is, the adage "Garbage in Garbage out" is always prevails.

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